

07 Dec 11

Answer:  $\uparrow$   
Today PT. Prof dep. h. av. R&R 5  
A duality <sup>to prepare</sup> <sup>in</sup> RDU, <sup>to model every individual</sup> <sup>confusing</sup> all <sup>novices</sup>

KT 200  
✓  
Anton

We argued: do not transform  
fixed-over-prob. one.

goodnews-prob. ranks.

Imagine alternative.

Some one says: "No, you are wrong"  
Better bad-news events!

~~margin of revolution~~  
~~in H. Neer~~  
~~which was~~  
~~lost~~

bring  
with  
five

loss-rank  $l$ : prob. getting  
outcome ranked  
worse.

loss-ranked prob:  $P_{rel} = P_e \text{ iso } P^n$

igo  
w

Take  $\alpha: [0,1] \rightarrow [0,1]$   
 $p_1, x_1 \dots p_n, x_n$  with  $x_1 \geq \dots \geq x_n$

$$\sum \pi_j U(x_j)$$

$\downarrow$

$$2 (p_1 + \dots + p_n) - 2 (p_{j+1} + \dots + p_n)$$

Marginal  $\Delta$  contribution of  
 $p_j$  to  $p_1 + \dots + p_n$

Why not??

Answer: Does not matter!  
Is the same!

$\lambda$  &  $w$  are each others' duals:

$$\lambda(p) = 1 - w(1-p); \text{ or:}$$

$$w(p) = 1 - \lambda(1-p)$$

$w$  is rank-weighter  
 $\lambda$  is loss-rank-weighter

$$p_1 \dots p_{j-1} p_j p_{j+1} \dots p_n$$

$$w(p_{j+1} + \dots + p_n) - w(p_{j-1} + \dots + p_n) =$$

$$1 - \lambda(p_{j+1} + \dots + p_n) - (1 - \lambda(p_{j-1} + \dots + p_n)) =$$

$$\lambda(p_{j-1} + \dots + p_n) - \lambda(p_{j+1} + \dots + p_n)$$

Fig 7.6.1, p. 220.  $r = p_1 + \dots + p_{j-1}$ ,  $l = p_{j+1} + \dots + p_n$

later, for PT, we will use  $\lambda$  early  
loss-ranks for losses. papers

Just as matter of convenience.  
Our critic was not criticizing us. Was saying  
the same thing.

2017

10:40 - 10:50

3

10:15 - 10:25

§ 8.1, Fig 8.1.1

Fig 6 nu geheel rechts tekenen.

culpriti?

(2017: Did not raise this question early enough, because discussion went nicely differently)

Empirical explanation:

reference dependence.

Ch. 8 NOT MUCH THEORY

Most important: loss aversion.

Here is the modeling of ref. dep. (yes without saying much about W) notation  
ref point  $0 = 0$

$u: \mathbb{R} \rightarrow \mathbb{R}$  : basic utility  
scaling:  $u(0) = 0$ .  
loss aversion

Overall utility  $U$ :

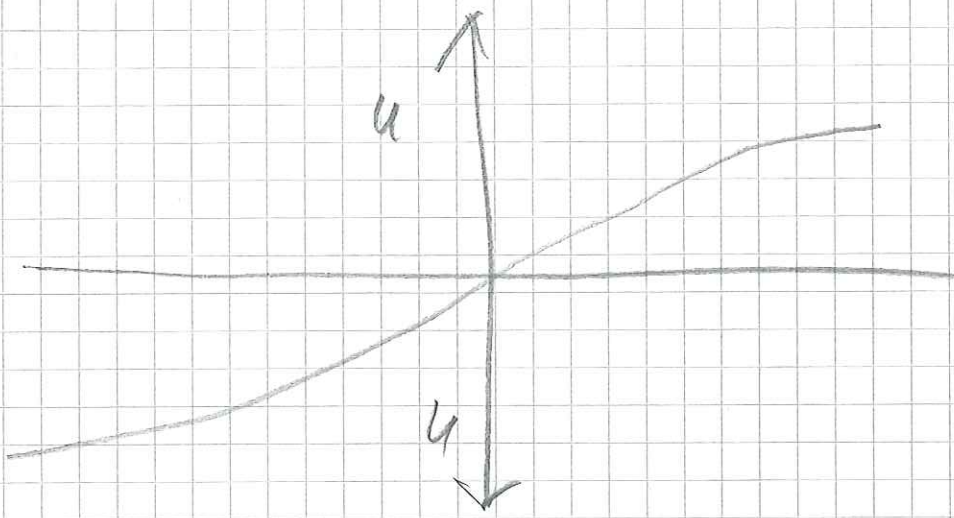
$$\alpha \geq 0: U(\alpha) = u(\alpha)$$

$$\alpha < 0: U(\alpha) = \lambda u(\alpha)$$

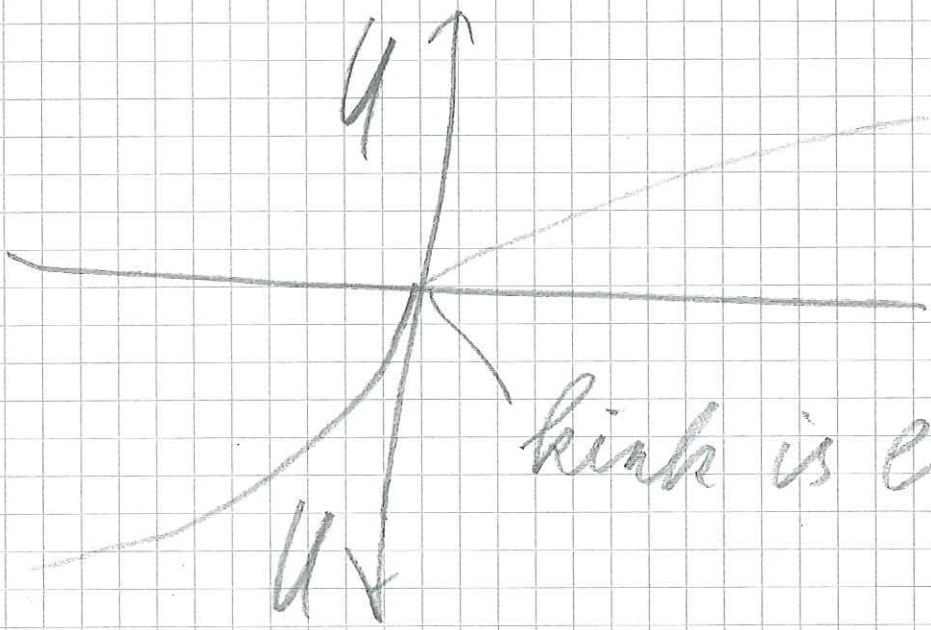
$$\text{also } U(0) = 0$$

loss aversion:  $\lambda \geq 1$

Can do ref-dep generalization of EU.

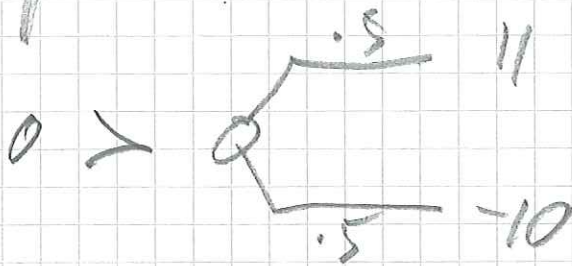


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kink is loss av.

# Rabin's paradox

Assume  $0 > \alpha$   (\*)

At every wealth level  $m$ .

Reference dependence through  
subscript in  $U_m$

No prob weighting for now.

(\*)  $\Rightarrow$

$$U_m(11) - U_m(\alpha) < U_m(\alpha) - U_m(-10)$$

So: every  $U_m$  moderately concave  
around  $\alpha$

That's it!

Classical Researcher <sup>What would happen to you if had you not taken my course?</sup> does not recognize reference dependence. Does

Think: final wealth, regular (concave)  $U$  (as in most of your other courses)

$$U(m+11) - U(m) < U(m) - U(m-10)$$

$$\frac{U(m+11) - U(m)}{11} < \frac{U(m) - U(m-10)}{10}$$

$$U'(m+11) < \frac{10}{11} U'(m-10)$$

$\forall m$ : Not plausible!

$U'$  dropping by  $\frac{10}{11}$  over every

increase by 21 ??

Over 210 by  $(\frac{10}{11})^{10} \approx 0.4$

Over 2100 by factor

Bomb always  $(\frac{10}{11})^{100} = 0.0001$  ??

Rabin showed it.

Refuse  $\forall M > 0$   $\forall M$  ???

Ref. Dep: Almost no theory yet.

Ex. 7.1: Assume no w.

R. av. & U not concave:

$\alpha$  vs  $P$ :

take  $\alpha$  as ref point. (plausible)

U steeper for losses than for gains.  $\Rightarrow$

$0 \geq P$  whenever  $EV(P) = 0$   
say for all  $\alpha$ :  $\Rightarrow$   
 $0 \geq_{\alpha} P$  " " " "

implies

But now  $\beta \geq_{\alpha} P$

for  $\beta \neq \alpha$  meaningless.  
 $\geq_{\alpha}$  not complete. We need new theory!  
New theories! Bleichrode...



Kőszegi & Rabin first operational theory.

We, From now on theory  
with fixed ref. point.  
Still completeness ...

Ch. 9. PJ

Ch. 9. P T (11:13 - 11:23) 10

Although no ref. dep.,  
still sign dep. Gains & losses

Now:  $U_{01R^+}$ ,  $U_{01R^-}$ ,  $w^+$ ,  $w^-$ ,  $\lambda$

Symmetries about 0 plausible.

To illustrate:

$$U(1020) - U(1010) < U(20) - U(10)$$

How about

$$U(-1010) - U(-1020) \quad U(-10) - U(-20)?$$

Economists:

$$U \text{ & } P T: > ! \\ < !$$

$U$  convex on  $(-\infty, 0)$ !  
Flies in face of classical  $E_{KPT}$  - Jaspe - rance

$W^+$ : Too gains, (gain - ranks);  
Being remote from 0 (ref. point)  
look from 0 up!

Symmetric for losses:

Look from 0 down!  
Relax everything to 0.

So, for losses, loss-ranks  
 $\approx$  gain-ranks.

Although formally equivalent,  
more natural to use loss-ranks  
for losses.

$W^-$  as loss-rank w. from

$\approx$   $W^+$

If  $W^+$  underweights gain-ranks  
(pessimism):

$W^-$  underweights loss-ranks.  
(optimism)

Reflection: u & w do it.

More risk av. for gains  $\Rightarrow$   
more risk seeking for losses.

See Figure 8.1.1. (the opening  
paradox in  
Ch. 8)

Def. PT:  $\exists U, u, \lambda, w^+, w^-$   
s.t.

$$x = p_1 x_1 + \dots + p_n x_n$$

Complexly sign-ranked:

$$x_1 \geq \dots \geq x_k \geq 0 \geq x_{k+1} \geq \dots \geq x_n$$

$$PT(x) = \sum_{j=1}^n \pi_j U(x_j)$$

$$x_i > 0 \quad (i \leq k):$$

$$\pi_i = \pi(p_i^{p_{i+1}} \dots p_{i-1}) = w^+(p_i + \dots + p_n) - w^+(p_{i+1} + \dots + p_n)$$

$$x_j < 0:$$

$$\pi_j = \pi(p_j^{p_{j+1}} \dots p_n) = w^-(p_j + \dots + p_n) - w^-(p_{j+1} + \dots + p_n)$$

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$$x = x^+ + x^- \quad (\text{defined})$$

$$PT(x) = PT(x^+) + PT(x^-)$$

Is sum of two differences  
RDU  $\frac{1}{2}$

$\mathbb{R}_+$  need not add to 1. 16

Violates monotony, as  
did old Edwards?

No!

Measuring  $U$  on  $\mathbb{R}_+$ ; just say

$U$  on  $\mathbb{R}_-$  the same

$\lambda$ , pragmatic:

$$\alpha_{\frac{1}{2}}(-1) \approx 0 \Rightarrow \alpha = \lambda$$

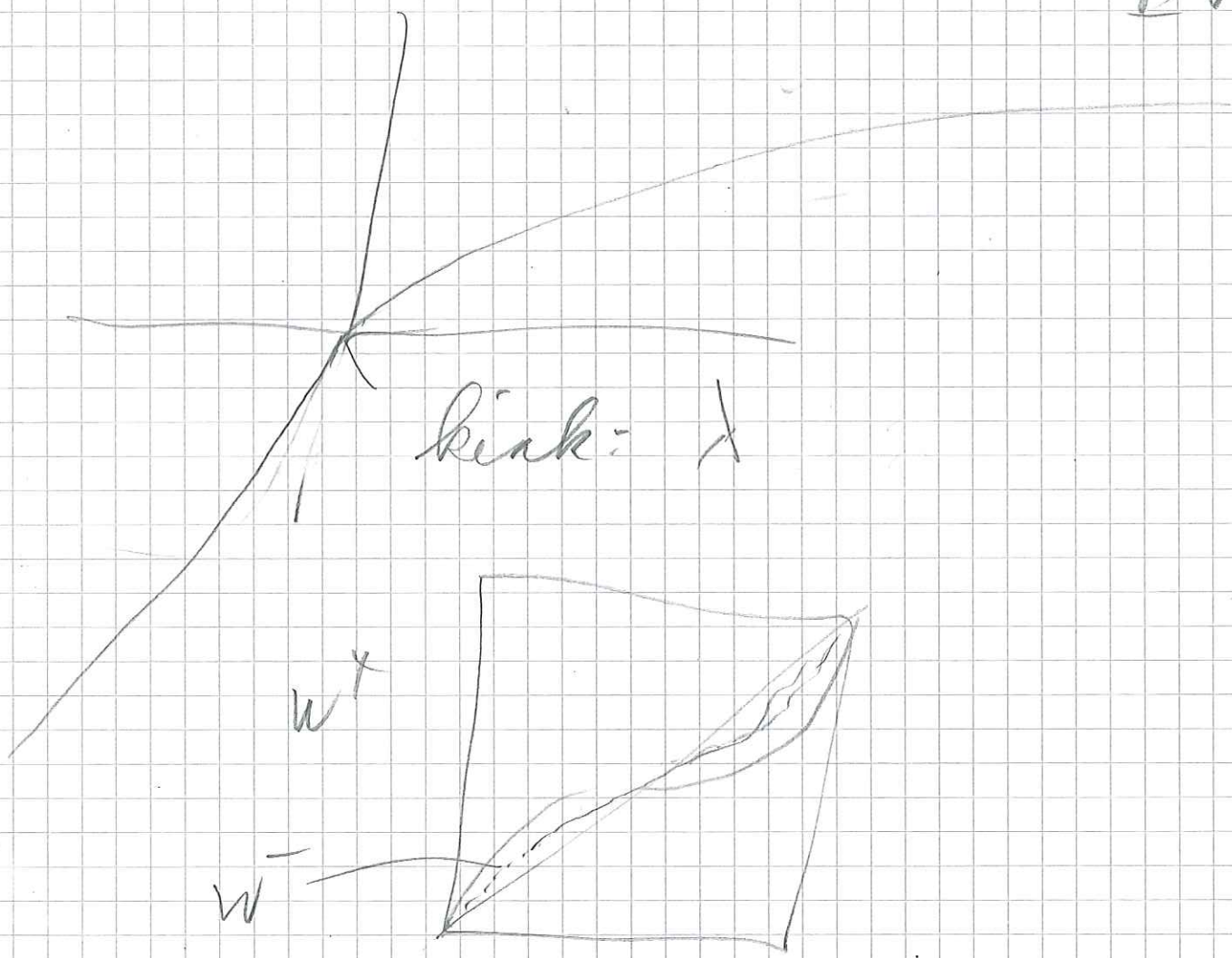
$$\cancel{w^+(\frac{1}{2})} U(\alpha) + \cancel{w^-(\frac{1}{2})} U(-1) = 0$$

$$U(\alpha) + \lambda U(-1) = 0$$

$$U \approx \text{linear} \\ \alpha - \lambda = 0$$

# 9.5. Empirical findings

reflection for losses,  
but less pronounced, closer to  
EV.



4. Gold prices

|

$\lambda \approx 2$

volatile ...

(more than  $w$ ,

more than  $U$ )

pragmatic: For gains:  $U$  say  $1 - \exp^{-\theta d}$

losses:  $U(d) = -U(-d)$

$\lambda$

$w^- = w^+ = T \& K$  92

3 parameters